# Classification Naïve Bayes 

UROŠ KRČADINAC
EMAIL: uros@krcadinac.com
URL: http://krcadinac.com

## Bayes rule

$$
P(H \mid E)=\frac{P(E \mid H) * P(H)}{P(E)}
$$

- H-hypothesis
- E - evidence related to the hypothesis H, i.e., the data to be used for validating (accepting/rejecting) the hypothesis H
- $\mathrm{P}(\mathrm{H})$ - probability of the hypothesis (prior probability)
- $\mathrm{P}(\mathrm{E})$ - probability of the evidence i.e., the state of the world described by the gathered data
- $\mathrm{P}(\mathrm{E} \mid \mathrm{H})$ - (conditional) probability of evidence E given that the hypothesis H holds
- $\mathrm{P}(\mathrm{H} \mid \mathrm{E})$ - (conditional) probability of the hypothesis H given the evidence E


## Naive Bayes classifier

- Lets make an assumption that all attributes are mutually independent:

$$
P(H \mid E)=\frac{P\left(E_{1} \mid H\right) * P\left(E_{2} \mid H\right) * \ldots * P\left(E_{n} \mid H\right) * P(H)}{P(E)}
$$

## Naive Bayes

- Makes two "naïve" assumptions over attributes:
- all attributes are a priori equally important
- all attributes are statistically independent (value of one attribute is not related to a value of another attribute)
- This assumptions mostly are not true, but in practice the algorithm gives good results

Example - Predicting whether a theater play will be performed

ToPlayOtNotToPlay.arff

| Outlook | Temp. | Humidity | Windy | Play |
| :---: | :---: | :---: | :---: | :---: |
| sunny | hot | high | false | no |
| sunny | hot | high | true | no |
| overcast | hot | high | false | yes |
| rainy | mild | high | false | yes |
| rainy | cool | normal | false | yes |
| rainy | cool | normal | true | no |
| overcast | cool | normal | true | yes |
| sunny | mild | high | false | no |
| sunny | cool | normal | false | yes |
| rainy | mild | normal | false | yes |
| sunny | mild | normal | true | yes |
| overcast | mild | high | true | yes |
| overcast | hot | normal | false | yes |
| rainy | mild | high | true | no |

## Sunny weather

Suppose you know that it is sunny outside

Then 60\% chance that
Play = no

| Outlook | Temp. | Humidity | Windy | Play |
| :---: | :---: | :---: | :---: | :---: |
| sunny | hot | high | false | no |
| sunny | hot | high | true | no |
| overcast | hot | high | false | yes |
| rainy | mild | high | false | yes |
| rainy | cool | normal | false | yes |
| rainy | cool | normal | true | no |
| overcast | cool | normal | true | yes |
| sunny | mild | high | false | no |
| sunny | cool | normal | false | yes |
| rainy | mild | normal | false | yes |
| sunny | mild | normal | true | yes |
| overcast | mild | high | true | yes |
| overcast | hot | normal | false | yes |
| rainy | mild | high | true | no |

How well does outlook predict play?

| Outlook | Temp. | Humidity | Windy P | Play |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| sunny | hot | high | false | no |  |
| sunny | hot | high | true | no |  |
| overcast | hot | high | false | yes |  |
| rainy | mild | high | false | yes |  |
| rainy | cool | normal | $\mathrm{f}^{-1}$ | Play |  |
| rainy | cool | normal | $t$ |  |  |
| overcast | cool | normal | Outlook | yes | no |
| sunny | mila | high | Outlook | yes |  |
| sunny | cool | normal | sunny | 2 | 3 |
| rainy | mild | normal | overcast | 4 | 0 |
| sunny | mild | normal | overcast |  | 0 |
| overcast | mild | high | rainv | 3 | 2 |
| overcast | hot | normal | TOTAL |  |  |
| rainy | mild | high |  | 9 | 5 |

How well does outlook predict play?


| Outlook | Temp. | Humidity | Windy | Play |
| :---: | :---: | :---: | :---: | :---: |
| sunny | hot | high | false | no |
| sunny | hot | high | true | no |
| overcast | hot | high | false | yes |
| rainy | mild | high | false | yes |
| rainy | cool | normal | false | yes |
| rainy | cool | normal | true | no |
| overcast | cool | normal | true | yes |
| sunny | mild | high | false | no |
| sunny | cool | normal | false | yes |
| rainy | mild | normal | false | yes |
| sunny | mild | normal | true | yes |
| overcast | mild | high | true | yes |
| overcast | hot | normal | false | yes |
| rainy | mild | high | true | no |

For each attribute ...

|  | Play |  |  | Play |  |  | Play |  |  | Play |  |  | Play |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Outlook | yes | no | Temp. | yes | no | Humid. | yes | no | Windy | yes | no |  |  |
| sunny | 2 | 3 | hot | 2 | 2 | high | 3 | 4 | false | 6 | 2 | yes | 9 |
| overcast | 4 | 0 | mild | 4 | 2 | normal | 6 | 1 | true | 3 | 3 | no | 5 |
| rainy | 3 | 2 | cool | 3 | 1 |  |  |  |  |  |  |  |  |
| TOTAL | 9 | 5 | TOTAL | 9 | 5 | TOTAL | 9 | 5 | TOTAL | 9 | 5 | TOTAL | 14 |

Values to ratios

|  | Play |  |  | Play |  |  | Play |  |  | Play |  |  | Play |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Outlook | yes | no | Temp. | yes | no | Humid. | yes | no | Windy | yes | no |  |  |
| sunny | 2 | 3 | hot | 2 | 2 | high | 3 | 4 | false | 6 | 2 | yes | 9 |
| overcast | 4 | 0 | mild | 4 | 2 | normal | 6 | 1 | true | 3 | 3 | no | 5 |
| rainy | 3 | 2 | cool | 3 | 1 |  |  |  |  |  |  |  |  |
| TOTAL | 9 | 5 | TOTAL | 9 | 5 | TOTAL | 9 | 5 | TOTAL | 9 | 5 | TOTAL | 14 |

Covert values to ratios

|  | Play |  |  | Play |  |  | Play |  |  | Play |  |  | Play |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Outlook | yes | no | Temp. | yes | no | Humid. | yes | no | Windy | yes | no |  |  |
| sunny | 0.22 | 0.60 | hot | 0.22 | 0.40 | high | 0.33 | 0.80 | false | 0.67 | 0.40 | yes | 0.64 |
| overcast | 0.44 | 0.00 | nild | 0.44 | 0.40 | normal | 0.67 | 0.20 | true | 0.33 | 0.60 | no | 0.36 |
| rainy | 0.33 | 0.40 | ool | 0.33 | 0.20 |  |  |  |  |  |  |  |  |

2 occurences of Play = no, where Outlook = rainy 5 occurences Play = no

## Likelihood of playing under these weather conditions

Calculate the likelihood that:
Outlook = sunny (0.22)
Temperature $=\operatorname{cool}(0.33)$
Humidity $=$ high (0.33)
Windy $=$ true (0.33)
Play $=$ yes (0.64)

Likelihood of playing under these weather conditions

$$
0.22 \times 0.33 \times 0.33 \times 0.33 \times 0.64=\mathbf{0 . 0 0 5 3}
$$

|  | Play |  |  | Play |  |  | Play |  |  | Play |  |  | Play |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Outlook | yes | no | Temp. | yes | no | Humid. | yes | no | Windy | yes | no |  |  |
| sunny | 0.22 | 0.60 | hot | 0.22 | 0.40 | high | 0.33 | 0.80 | false | 0.67 | 0.40 | yes | 0.64 |
| overcast | 0.44 | 0.00 | mild | 0.44 | 0.40 | normal | 0.67 | 0.20 | true | 0.33 | 0.60 | no | 0.36 |
| rainy | 0.33 | 0.40 | cool | 0.33 | 0.20 |  |  |  |  |  |  |  |  |

## Likelihood of NOT playing under these weather conditions

Calculate the likelihood that:
Outlook = sunny (0.60)
Temperature $=\operatorname{cool}(0.20)$
Humidity $=$ high ( 0.80 )
Windy $=$ true ( 0.60 )
Play $=$ no (0.36)

Likelihood of NOT playing under these weather conditions

$$
0.60 \times 0.20 \times 0.80 \times 0.60 \times 0.36=\mathbf{0 . 0 2 0 6}
$$

|  | Play |  |  | Play |  |  | Play |  |  | Play |  |  | Play |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Outlook | yes | no | Temp. | yes | no | Humid. | yes | no | Windy | yes | no |  |  |
| sunny | 0.22 | 0.60 | hot | 0.22 | 0.40 | high | 0.33 | 0.80 | false | 0.67 | 0.40 | yes | 0.64 |
| overcast | 0.44 | 0.00 | mild | 0.44 | 0.40 | normal | 0.67 | 0.20 | true | 0.33 | 0.60 | no | 0.36 |
| rainy | 0.33 | 0.40 | cool | 0.33 | 0.20 |  |  |  |  |  |  |  |  |

## The Bayes Theorem

Given these weather conditions:
Outlook = sunny
Temperature = cool
Humidity = high
Windy = true

Probability of Play = yes:

$$
\frac{0.0053}{0.0053+0.0206}=20.5 \%
$$

Probability of Play = no:

$$
\frac{0.0206}{0.0053+0.0206}=79.5 \%
$$

$P(H \mid E)=\frac{P\left(E_{1} \mid H\right) * P\left(E_{2} \mid H\right) * \ldots * P\left(E_{n} \mid H\right) * P(H)}{P(E)}$

## Likelihood of NOT playing under these weather conditions

Calculate the likelihood that:
Outlook = ovecast (0.00)
Temperature $=\operatorname{cool}(0.20)$
Humidity $=$ high (0.80)
Windy $=$ true ( 0.60 )
Play $=$ no (0.36)
$0.00 \times 0.20 \times 0.80 \times 0.60 \times 0.36=\mathbf{0 . 0 0 0 0}$

|  | Play |  |  | Play |  |  | Play |  |  | Play |  |  | Play |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Outlook | yes | no | Temp. | yes | no | Humid. | yes | no | Windy | yes | no |  |  |
| sunny | 0.22 | 0.60 | hot | 0.22 | 0.40 | high | 0.33 | 0.80 | false | 0.67 | 0.40 | yes | 0.64 |
| overcast | 0.44 | 0.00 | mild | 0.44 | 0.40 | normal | 0.67 | 0.20 | true | 0.33 | 0.60 | no | 0.36 |
| rainy | 0.33 | 0.40 | cool | 0.33 | 0.20 |  |  |  |  |  |  |  |  |

## Laplace estimator

The original dataset

|  | Play |  |  | Play |  |  | Play |  |  | Play |  |  | Play |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Outlook | yes | no | Temp. | yes | no | Humid. | yes | no | Windy | yes | no |  |  |
| sunny | 2 | 2 | hot | 2 | 2 | high | 3 | 4 | false | 6 | 2 | yes | 9 |
| overcast | 4 | 0 | mild | 4 | 2 | normal | 6 | 1 | true | 3 | 3 | no | 5 |
| rainy | 3 |  | cool | 3 | 1 |  |  |  |  |  |  |  |  |
| TOTAL | 9 |  | TOTAL | 9 | 5 | TOTAL | 9 | 5 | TOTAL | 9 | 5 | TOTAL | 14 |

Laplace estimator:
Add 1 to each count

After the Laplace estimator

|  | Play |  |  | Play |  |  | Play |  |  | Play |  |  | Play |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Outlook | yes | no | Temp. | yes | no | Humid. | yes | no | Windy | yes | no |  |  |
| sunny | 3 |  | hot | 3 | 3 | high | 4 | 5 | false | 7 | 3 | yes | 12 |
| overcast | 5 | 1 | nild | 5 | 3 | normal | 7 | 2 | true | 4 | 4 | no | 8 |
| rainy | 4 | 3 | cool | 4 | 2 |  |  |  |  |  |  |  |  |
| TOTAL | 12 | 8 | TOTAL | 12 | 8 | TOTAL | 11 | 7 | TOTAL | 11 | 7 | TOTAL | 20 |

## Laplace estimator

|  | Play |  | Temp. | Play |  | Humid. | Play |  | Windy | Play |  |  | Play |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Outlook | yes | no |  | yes | no |  | yes | no |  | yes | no |  |  |
| sunny | 3 | 4 | hot | 3 | 3 | high | 4 | 5 | false | 7 | 3 | yes | 9 |
| overcast | 5 | 1 | mild | 5 | 3 | normal | 7 | 2 | true | 4 | 4 | no | 5 |
| rainy | 4 | 3 | cool | 4 | 2 |  |  |  |  |  |  |  |  |
| TOTAL | 12 | 8 | TOTAL | 12 | 8 | TOTAL | 11 | 7 | TOTAL | 11 | 7 | TOTAL | 14 |

Convert incremented counts to ratios after implementing the Laplace estimator

|  | Play |  | Temp. | Play |  | Humid. | Play |  | Windy | Play |  |  | Play |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Outlook | yes | no |  | yes | no |  | yes | no |  | yes | no |  |  |
| sunny | 0.25 | 0.50 | hot | 0.25 | 0.38 | high | 0.36 | 0.71 | false | 0.64 | 0.43 | yes | 0.64 |
| overcast | 0.42 | 0.13 | mild | 0.42 | 0.38 | normal | 0.64 | 0.29 | true | 0.36 | 0.57 | no | 0.36 |
| rainy | 0.33 | 0.38 | cool | 0.33 | 0.25 |  |  |  |  |  |  |  |  |

## Laplace estimator

|  | Play |  |  | Play |  |  | Play |  |  | Play |  |  | Play |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Outlook | yes | no | Temp. | yes | no | Humid. | yes | no | Windy | yes | no |  |  |
| sunny | 0.25 | 0.50 | hot | 0.25 | 0.38 | high | 0.36 | 0.71 | false | 0.64 | 0.43 | yes | 0.64 |
| overcast | 0.42 | 0.13 | mild | 0 O | 038 | normal | 0.64 | 0.29 | true | 0.36 | 0.57 | no | 0.36 |
| rainy | 0.33 | 0.38 | cool | 033 | 025 |  |  |  |  |  |  |  |  |

Outlook $=$ ovecast, Temperature $=$ cool, Humidity $=$ high, Windy $=$ true

$$
\begin{aligned}
& \text { Play }=\text { no: } 0.13 \times 0.25 \times 0.71 \times 0.57 \times 0.36=0.046 \\
& \text { Play }=\text { yes: } 0.42 \times 0.33 \times 0.36 \times 0.36 \times 0.64=0.0118
\end{aligned}
$$

Probability of Play = no:

$$
\frac{0.0046}{0.0046+0.0118}=28 \%
$$

Probability of Play = yes:

$$
\frac{0.0118}{0.0046+0.0118}=72 \%
$$

## Laplace estimator

Under these weather conditions:
Temperature = cool
Humidity = high
Windy = true

NOT using Laplace estimator:
Play = no: 79.5\%
Play = yes: $20.5 \%$

Using Laplace estimator:
Play = no: 72.0\%
Play = yes: $28.0 \%$

The effect of Laplace estimator has little effect as sample size grows.

## Prediction rules

| Outlook | Temp. | Humid. | Windy | Play |
| :--- | :---: | :---: | :---: | :---: |
| overcast | cool | high | false | no |
| overcast | cool | high | false | yes |
| overcast | cool | high | true | no |
| overcast | cool | high | true | yes |
| overcast | cool | normal | false | no |
| overcast | cool | normal | false | yes |
| overcast | cool | normal | true | no |
| overcast | cool | normal | true | yes |
| overcast | hot | high | false | no |
| overcast | hot | high | false | yes |
| overcast | hot | high | true | no |
| overcast | hot | high | true | yes |
| overcast | hot | normal | false | no |
| overcast | hot | normal | false | yes |
| overcast | hot | normal | true | no |
| overcast | hot | normal | true | yes |

Repeat previous calculation for all other combinations of weather conditions.

Calculate the rules for each pair.
Then throw out the rules with

$$
p<0.5
$$

## Prediction rules

|  | Play |  |  | Play |  |  | Play |  |  | Play |  |  | Play |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Outlook | yes | no | Temp. | yes | no | Humid. | yes | no | Windy | yes | no |  |  |
| sunny | 0.25 | 0.50 | hot | 0.25 | 0.38 | high | 0.36 | 0.71 | false | 0.64 | 0.43 | yes | 0.64 |
| overcast | 0.42 | 0.13 | mild | 0.42 | 0.38 | normal | 0.64 | 0.29 | true | 0.36 | 0.57 | no | 0.36 |
| rainy | 0.33 | 0.38 | cool | 0.33 | 0.25 |  |  |  |  |  |  |  |  |


| Inst | Outlook | Temp. | Humid. | Windy | Play | Outlook | Temp. | Humid. | Windy | Play | Like. | Prob. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | overcast | cool | high | false | no | 0.13 | 0.25 | 0.71 | 0.43 | 0.36 | 0.0034 | 14.2\% |
|  | overcast | cool | high | false | yes | 0.42 | 0.33 | 0.36 | 0.64 | 0.64 | 0.0207 | 85.8\% |
|  | overcast | cool | high | Calculate probabilities for all 36 combinations |  |  |  | 0.71 | 0.57 | 0.36 | 0.0046 | 27.8\% |
|  | overcast | cool | high |  |  |  |  | 0.36 | 0.36 | 0.64 | 0.0118 | 72.2\% |
|  | overcast | cool | normal |  |  |  |  | 0.29 | 0.43 | 0.36 | 0.0014 | 3.6\% |
|  | overcast | cool | normal | false | yes | 0.42 | 0.33 | 0.64 | 0.64 | 0.64 | 0.0362 | 96.4\% |
|  | overcast | cool | normal | true | no | 0.13 | 0.25 | 0.29 | 0.57 | 0.36 | 0.0018 | 8.1\% |
| 7 | overcast | cool | normal | true | yes | 0.42 | 0.33 | 0.64 | 0.36 | 0.64 | 0.0207 | 91.9\% |
|  | overcast | hot | high | false | no | 0.13 | 0.38 | 0.71 | 0.43 | 0.36 | 0.0051 | 24.9\% |
| 3 | overcast | hot | high | false | yes | 0.42 | 0.25 | 0.36 | 0.64 | 0.64 | 0.0155 | 75.1\% |

## Prediction rules

| Inst | Outlook | Temp. | Humid. | Windy | Play | Prob. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | overcast | cool | normal | false | yes | $96.4 \%$ |
|  | overcast | mild | normal | false | yes | $95.7 \%$ |
| 13 | overcast | hot | normal | false | yes | $93.0 \%$ |
| 7 | overcast | cool | normal | true | yes | $91.9 \%$ |
|  | overcast | mild | normal | true | yes | $90.4 \%$ |
| 5 | rainy | cool | normal | false | yes | $87.6 \%$ |
|  | overcast | cool | high | false | yes | $85.8 \%$ |
| 10 | rainy | mild | normal | false | yes | $85.5 \%$ |
|  | overcast | hot | normal | true | yes | $85.0 \%$ |
| 2 | sunny | hot | high | true | no | $83.7 \%$ |
|  | overcast | mild | high | false | yes | $83.4 \%$ |
| 9 | sunny | cool | normal | false | yes | $79.9 \%$ |
|  | rainy | hot | normal | false | yes | $77.9 \%$ |
|  | sunny | mild | normal | false | yes | $76.8 \%$ |
|  | sunny | mild | high | true | no | $75.5 \%$ |
| 3 | overcast | hot | high | false | yes | $75.1 \%$ |
|  | rainy | cool | normal | true | yes | $75.1 \%$ |
|  | rainy | hot | high | true | no | $74.3 \%$ |


| Inst | Outlook | Temp. | Humid. | Windy | Play | Prob. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | avercast | cool | high | true | yes | $72.2 \%$ |
|  | sunny | cool | high | true | no | $72.0 \%$ |
|  | rainy | mild | normal | true | yes | $71.6 \%$ |
| 1 | sunny | hat | high | false | no | $68.8 \%$ |
| 12 | avercast | mild | high | true | yes | $68.4 \%$ |
|  | sunny | hat | normal | false | yes | $66.5 \%$ |
| 14 | rainy | mild | high | true | no | $63.5 \%$ |
|  | sunny | cool | normal | true | yes | $63.0 \%$ |
|  | rainy | cool | high | false | yes | $61.7 \%$ |
|  | rainy | hat | normal | true | yes | $60.2 \%$ |
|  | rainy | cool | high | true | no | $59.1 \%$ |
| 11 | sunny | mild | normal | true | yes | $58.6 \%$ |
| 4 | rainy | mild | high | false | yes | $57.3 \%$ |
| 8 | sunny | mild | high | false | no | $57.0 \%$ |
|  | avercast | hat | high | true | yes | $56.4 \%$ |
|  | rainy | hat | high | false | no | $55.4 \%$ |
|  | sunny | hat | normal | true | no | $54.0 \%$ |
|  | sunny | cool | high | false | no | $52.4 \%$ |

Rules predicting class for all combinations of attributes

## Comparing the prediction with the original data

| Inst | Outlook | Temp. | Humid. | Windy | Play | Prob. | Actual |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | sunny | hot | high | false | no | $72.6 \%$ | no |
| 2 | sunny | hot | high | true | no | $86.1 \%$ | no |
| 3 | overcast | hot | high | false | yes | $71.6 \%$ | yes |
| 4 | rainy | mild | high | false | yes | $52.8 \%$ | yes |
| 5 | rainy | cool | normal | false | yes | $85.5 \%$ | yes |
| 6 | rainy | cool | normal | true | yes | $75.1 \%$ | no |
| 7 | overcast | cool | normal | true | yes | $90.4 \%$ | yes |
| 8 | sunny | mild | high | false | no | $61.4 \%$ | no |
| 9 | sunny | cool | normal | false | yes | $76.8 \%$ | yes |
| 10 | rainy | mild | normal | false | yes | $83.0 \%$ | yes |
| 11 | sunny | mild | normal | true | yes | $54.2 \%$ | yes |
| 12 | overcast | mild | high | true | yes | $64.3 \%$ | yes |
| 13 | overcast | hot | normal | false | yes | $91.7 \%$ | yes |
| 14 | rainy | mild | high | true | no | $67.6 \%$ | no |

## Naïve Bayes in Weka



## Predictions over training dataset

## ToPlayOtNotToPlay.arff dataset



## Classification results

|  | Play |  |  | Play |  |  | Play |  |  | Play |  |  | Play |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Outlook | yes | no | Temp. | yes | no | Humid. | yes | no | Windy | yes | no |  |  |
| sunny | 3 | 4 | ot | 3 | 3 | high | 4 | 5 | false | 7 | 3 | yes | 12 |
| overcast | 5 | 1 | nild | 5 | 3 | normal | 7 | 2 | Classifier output |  |  |  |  |
| rainy | 4 | 3 | ool | 4 | 2 |  |  |  | Attribute |  | $\begin{array}{r} \text { no } \\ (0.38) \end{array}$ |  |  |
| TOTAL | 12 | 8 | IOTAL | 12 | 8 | TOTAL | 11 | 7 |  |  |  |  |

> Outlook
sunny $4.0 \quad 3.0$
overcast
$1.0 \quad 5.0$
rainy
$3.0 \quad 4.0$
[total]
8.0
12.0

Temp.

| hot | 3.0 | 3.0 |
| :--- | ---: | ---: |
| mild | 3.0 | 5.0 |
| cool | 2.0 | 4.0 |
| [total] | 8.0 | 12.0 |

The Laplace estimator is automatically applied

## Classification results



## Naïve Bayes features

- Intended primarily for the work with nominal attributes
- In case of numeric attributes:
- Use the probability distribution of attributes (Normal distribution is default) for probability estimation for the each attribute
- Discretize the attribute's values


## Example 2 - Eatable Mushrooms dataset

EdibleMushrooms.arff

- Eatable Mushrooms dataset based on "National Audubon Society Field Guide to North American Mushrooms"
- Hypothetical samples with descriptions corresponding to 23 species of mushrooms
- There are 8124 instances with 22 nominal attributes which describe mushroom characteristics; one of which is whether a mushroom is eatable or not
- Our goal is to predict whether a mushroom is eatable or not

Data in this dataset are hypothetical and these results are not to be used in real life!

## Baseline classifier

> diabetes.arff

- There are total of 768 instances ( 500 negative, 268 positive)
- A priori probabilities for classes negative and positive are

$$
\begin{aligned}
\text { Negativan } & =\frac{500}{768} \cdot 100 \%=65.1 \% \\
\text { Pozitivan } & =\frac{268}{768} \cdot 100 \%=34.9 \%
\end{aligned}
$$

- Baseline classifier classifies every instances to the dominant class, the class with the highest probability
- In Weka, the implementation of baseline classifier is: rules -> ZeroR


## Baseline classifier in Weka: rules -> ZeroR



## Baseline classifier

- Open dataset diabetes.arff
- Test option: Percentage split $66 \%$
- Test classifiers:
- rules -> ZeroR

65\%

- trees -> J48 76\%
- bayes -> NaiveBayes 77\%
- lazy -> Ibk 73\%
- For every classification problem test first whether the tested classifier performs better than the baseline classifier


## Example 3 - Supermarket dataset

- Dataset describes data about the article sales in a local supermarket in New Zealand in one day.
- Attributes are nominal and describes different store departments and different article categories (e.g. "bread and cake' refer to the group of baking products).
- Value " t " of an attributes means that the shopping cart contained at least one product for the specific department or at least one product from the product category.
- Class has values "low" and "high" determining whether a byer spent less or more than $100 \$$ for the shopping


## Recommendations and credits

Weka Tutorials and Assignments @ The Technology Forge

- Link: http://www.technologyforge.net/WekaTutorials/
"Data Mining with Weka" and "More Data Mining with Weka": MOOCs from the University of Waikato. A self-paced session of "Data Mining with Weka" runs until 23 October June 2015.
- Link: https://www.youtube.com/user/WekaMOOC/
(Anonymous) survey for your comments and suggestions: http://goo.gl/cqdp3|


## ANY QUESTIONS?

UROŠ KRČADINAC
EMAIL: uros@krcadinac.com
URL: http://krcadinac.com

